## VAISALA

## $\mathrm{H}_{2} \mathrm{O}_{2}$ Conversions

FORMULAS AND METHODS
FOR CALCULATING VAPORIZED
HYDROGEN PEROXIDE PARAMETERS


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## $\mathrm{H}_{2} \mathrm{O}_{2}$ conversions

## 1. Foreword

This document describes the functions and methods for calculating different humidity and vaporized hydrogen peroxide variables. For information on measuring liquid hydrogen peroxide please see our Web page on Chemical Processing. As shown in the diagram below, the partial vapor pressure ( $P_{W} / P_{h}$ ) and saturation vapor pressure $\left(P_{w s} / P_{h s}\right)$ are the key factors in parametric calculations. Other parameters can be derived from these parameters by using functions, iterative methods, and auxiliary parameters: temperature and pressure. The units selected for this document are in accordance with the International System of Units (SI). Conversion to Imperial units can be found from chapter 11.


| $P_{w s}$ | $=$ | Saturation vapor pressure over water in Pa |
| :---: | :---: | :---: |
| $P_{\text {hs }}$ | $=$ | Saturation vapor pressure over hydrogen peroxide in Pa |
| $P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ | $=$ | Saturation vapor pressure over water in $\mathrm{H}_{2} \mathrm{O}_{2}$ environments in Pa |
| $P_{w} / P_{h}$ | $=$ | Vapor saturation pressure over water / hydrogen peroxide in Pa |
| RH | = | Relative humidity in \%rh |
| $R S$ | $=$ | Relative saturation in \%rs |
| $\mathrm{T}_{\mathrm{d}}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ | $=$ | Dew Point in ${ }^{\circ} \mathrm{C}$ |
| $a_{w}$ | $=$ | Absolute humidity in $\mathrm{g} / \mathrm{m}^{3}$ |
| $a_{h}$ | = | Absolute hydrogen peroxide in $\mathrm{mg} / \mathrm{m}^{3}$ |
| ppm | = | Parts per million (volume ${ }_{\text {H2O2 or }{ }^{\text {H2O }} \text { /volume }{ }_{\text {gas }} \text { ) }}$ |
| $p p m_{m}$ | $=$ | Parts per million (mass ${ }_{\text {H2O }} /$ mass $_{\text {gas }}$ ) |
| $F(T, p, M)$ | $=$ | Function with auxiliary quantities: temperature, pressure, or molar |
| $F^{n}(T, p)$ | $=$ | Iterative method with auxiliary quantities: temperature and pressure |

## 2. Water and $\mathrm{H}_{2} \mathrm{O}_{2}$ content - ppm (parts per million)

Parts per million is a unitless parameter typically used to state a small amount of chemical concentration. There are two different ways to express $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O}_{2}$ contents and care should be taken in this because, in both chemicals, contents may refer to either mass fraction or volume fraction. We describe differences in these expressions in the following chapters.

## $2.1 \mathrm{ppm}_{\mathrm{v}}$ - volume/volume

$$
p p m_{V}=\frac{P_{x}}{p} \cdot 10^{6}, \text { where }
$$

(Equation 1)
$P_{x}=$ Vapor pressure of chemical $X$ in Pa
$p=$ Total pressure in Pa

## Examples:

To calculate water vapor concentration in volume fraction ( $\mathrm{ppm}_{\mathrm{v}}$ ) in the following condition:

```
P
p = 101325 Pa
```

$\operatorname{ppm}_{V H 2 O}=\frac{P_{w}}{\mathrm{p}} \cdot 10^{6}=\frac{982.26 \mathrm{~Pa}}{101325 \mathrm{~Pa}} \cdot 10^{6}=9694 \mathrm{ppm}_{\mathrm{V}}$
To calculate $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor concentration in volume fraction ( $\mathrm{ppm}_{\mathrm{v}}$ ) in following condition:
$P_{h}=50.66 \mathrm{~Pa}$
$p=101325 \mathrm{~Pa}$
$\operatorname{ppm}_{V H 2 O 2}=\frac{P_{h}}{\mathrm{p}} \cdot 10^{6}=\frac{50.66 \mathrm{~Pa}}{101325 \mathrm{~Pa}} \cdot 10^{6}=500 \mathrm{ppm}_{\mathrm{v}}$
$2.2 \mathrm{ppm}_{\mathrm{m}}$ - mass/mass
ppm $_{m}=\frac{M_{\chi} \cdot P_{\chi}}{M_{\text {gas }} \cdot p} \cdot 10^{6}$, where
(Equation 2)
$M_{x}=$ Molecular weight of chemical X in g.mol${ }^{-1}\left(\mathrm{H}_{2} \mathrm{O}_{2}=34.0136 \mathrm{~g} \cdot \mathrm{~mol}^{-1}\right)^{1}$
$M_{\text {gas }}=$ Molecular weight of dry gas in g.mol${ }^{-1}(\text { air }=28.965)^{1}$

## Example:

To calculate $\mathrm{H}_{2} \mathrm{O}_{2}$ concentration in mass fraction (ppm ) in following condition:

```
M H2O2}=34.0136 g.mol-1
P
p=101325 Pa
```

ppm $_{\text {m }}{ }^{2 O 2}=\frac{34.0136 \mathrm{~g} \cdot \mathrm{~mol}^{-1} \cdot 50.66 \mathrm{~Pa}}{28.965 \mathrm{~g} \cdot \mathrm{~mol}^{-1} \cdot 101325 \mathrm{~Pa}} \cdot 10^{6}=587 \mathrm{ppm}_{\mathrm{m}}$

[^0]
## 3. Relative humidity - RH

Relative humidity indicates the humidity value derived from water vapor only. Relative humidity is defined at all temperatures and pressures as the ratio of the water vapor pressure $\left(P_{w}\right)$ to the saturation water vapor pressure over water ( $P_{\text {ws }}$ ) at the gas temperature:

$$
\begin{equation*}
R H=\frac{P_{w}}{P_{w s}} \cdot 100 \% r h \tag{Equation3}
\end{equation*}
$$

The total pressure does not enter the definition. Above $100^{\circ} \mathrm{C}$ the same definition is valid. But as the saturation vapor pressure $P_{w s}$ is greater than $1,013 \mathrm{hPa}$ (normal ambient pressure), the RH cannot reach $100 \%$ in an unpressurized system. This definition is also valid below $0^{\circ} \mathrm{C}$. Here $100 \%$ rh is impossible because condensation will occur at a lower humidity than $100 \%$ (when the vapor is saturated against ice).

## 4. Relative saturation - RS

Relative saturation indicates the humidity value derived from the combination of water vapor and hydrogen peroxide vapor. Relative saturation is defined at all temperatures and pressures as the ratio of the water vapor pressure $\left(P_{w}\right)$ to the saturation water vapor pressure at a given $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor concentration $\left(P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\right.\right.$ $\left.\mathrm{H}_{2} \mathrm{O}_{2}\right)$ ) at the gas temperature:

$$
R S=\frac{P_{w}}{P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)} \cdot 100 \% r s
$$

## Example:

To calculate RS in the following condition:

```
ppmv}\mp@subsup{\textrm{H}}{2}{}\mp@subsup{O}{2}{}=500 ppm
T = 20 }\mp@subsup{}{}{\circ}\textrm{C}=> \mp@subsup{\textrm{T}}{\textrm{k}}{}=293.15\textrm{K
RH = 42.0 %rh
p=101325 Pa
Pws}(\mp@subsup{\textrm{H}}{2}{}\textrm{O}+\mp@subsup{\textrm{H}}{2}{}\mp@subsup{\textrm{O}}{2}{})(17)=1068.85 Pa
P
```

Answer: $R S=92.50$ \%rs

## 5. Water vapor saturation pressure - $P_{\text {ws }}$

Water vapor saturation pressure indicates the maximum vapor pressure of pure water at a given temperature. At saturation vapor pressure, water is in thermodynamic equilibrium, meaning that its liquid and solid phases are in equilibrium. Many saturation vapor pressure equations exist to calculate the saturation pressure of water vapor over a surface of liquid water ( $P_{w s}$ ). Water vapor saturation pressure can be calculated using Sonntag's equation [1]. This equation is valid in temperature ranges from $0^{\circ} \mathrm{C}$ to $100^{\circ} \mathrm{C}$.

$$
\begin{equation*}
P_{w s}\left(T_{K}\right)=a_{0} \cdot \exp \left[\frac{a_{1}}{T_{K}}+a_{2}+a_{3} T+a_{4} T^{2}+a_{5} \ln \left(a_{6} \cdot T_{K}\right)\right], \text { where } \tag{Equation5}
\end{equation*}
$$

$P_{w s}=$ Saturation vapor pressure above water in Pa
$T_{K}=$ Temperature in K

Table 1: Numerical values for coefficients $a_{0} \ldots a_{6}$

| Coefficients $a_{n}$ | Above water $\left(P_{w s}\right)$ <br> $\left(0\right.$ to $\left.100{ }^{\circ} \mathrm{C}\right)$ |
| :---: | :---: |
| $a_{0}$ | $1[\mathrm{~Pa}]$ |
| $a_{1}$ | $-6.0969385 \mathrm{E}+03[\mathrm{~K}]$ |
| $a_{2}$ | $2.12409642 \mathrm{E}+01$ |
| $a_{3}$ | $-2.711193 \mathrm{E}-02\left[\mathrm{~K}^{-1}\right]$ |
| $a_{4}$ | $1.673952 \mathrm{E}-05\left[\mathrm{~K}^{-2}\right]$ |
| $a_{5}$ | 2.433502 |
| $a_{6}$ | $1\left[\mathrm{~K}^{-1}\right]$ |

## Example:

To calculate water vapor saturation pressure in $20^{\circ} \mathrm{C}$ temperature:

```
T=20 }\mp@subsup{}{}{\circ}\textrm{C}=> \mp@subsup{T}{K}{}=20+273.15=293.15\textrm{K
Pws}=2339.25 Pa
```


## 6. $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor saturation pressure - $P_{h s}$

Hydrogen peroxide vapor saturation pressure indicates the maximum vapor pressure of pure $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor at a given temperature. At saturation vapor pressure, hydrogen peroxide is in thermodynamic equilibrium, meaning that its liquid and gas phases are in equilibrium. The following equation by Scatchart et. al. can be used to calculate the saturation pressure of $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor over a surface of liquid $\mathrm{H}_{2} \mathrm{O}_{2}\left(P_{h s}\right)$ [2].

$$
P_{h s}\left(T_{K}\right)=\frac{10^{\left[a_{0}+\frac{a_{1}}{T}+a_{2} \cdot \log T+a_{3} \cdot T\right]}}{7.5006 \cdot 10^{-3}}, \text { where }
$$

$P_{h s}=$ Saturation vapor pressure above $\mathrm{H}_{2} \mathrm{O}_{2}$ in Pa
$T_{K}=$ Temperature in K

Table 2: Numerical values for coefficients $a_{0} \ldots a_{3}$

| Coefficients $\mathrm{a}_{\mathrm{n}}$ | Above $\mathrm{H}_{2} \mathrm{O}_{2}\left(\boldsymbol{P}_{h s}\right)$ |
| :---: | :---: |
| $\mathrm{a}_{0}$ | $44.576[\mathrm{~Pa}]$ |
| $\mathrm{a}_{1}$ | $-4025[\mathrm{~K}]$ |
| $\mathrm{a}_{2}$ | $-12.996\left[\mathrm{~K}^{-1}\right]$ |
| $\mathrm{a}_{3}$ | $0.004605\left[\mathrm{~K}^{-1}\right]$ |

## Example:

To calculate the $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor saturation pressure in $20^{\circ} \mathrm{C}$ temperature:

```
T = 20 }\mp@subsup{}{}{\circ}\textrm{C}=> \mp@subsup{T}{K}{}=20+273.15=293.15 
Phs}=181.30 Pa
```


## 7. Water vapor saturation pressure in an $\mathrm{H}_{2} \mathrm{O}_{2}$ environment $P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$

Water vapor saturation pressure $P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ in an environment that contains $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor indicates the maximum water vapor pressure when hydrogen peroxide vapor is present. Calculating water vapor saturation pressure in an $\mathrm{H}_{2} \mathrm{O}_{2}$ environment involves complex equations because the saturation point depends on hydrogen peroxide and water vapor concentrations, as well as temperature. To calculate water vapor saturations in these environments, we can derive the equation, $P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$, from Raoult's law. The equation is then solved through an iterative procedure.

### 7.1 Raoult's law for vapor pressure

Raoult's law for non-ideal vapor pressures states that partial pressure of each chemical $X\left(P_{X}\right)$ in a solution can be calculated:

$$
\begin{equation*}
P_{x}=\gamma_{x} \cdot x_{x} \cdot P_{x s}, \text { where } \tag{Equation7}
\end{equation*}
$$

$P_{x}=$ Vapor pressure of chemical $X$ in Pa
$Y_{x}=$ Activity coefficient of chemical $X$
$X_{x}=$ Mole fraction of chemical $X$
$P_{x s}=$ Saturation vapor pressure above chemical $X$ in Pa
Therefore, we can form similar equations for water and hydrogen peroxide respectively:
$P_{w}=\gamma_{w} \cdot x_{w} \cdot P_{w s}$ and $P_{h}=\gamma_{h} \cdot x_{h} \cdot P_{h s}$, where
(Equation 8,9)
$P_{w}=$ Vapor pressure of water in Pa
$P_{h}=$ Vapor pressure of $\mathrm{H}_{2} \mathrm{O}_{2}$ in Pa
$Y_{w}=$ Activity coefficient of water
$Y_{h}=$ Activity coefficient of $\mathrm{H}_{2} \mathrm{O}_{2}$
$X_{w}=$ Mole fraction of water
$X_{h}=$ Mole fraction of $\mathrm{H}_{2} \mathrm{O}_{2}$
$P_{w s}=$ Saturation vapor pressure above water in Pa
$P_{h s}=$ Saturation vapor pressure above $\mathrm{H}_{2} \mathrm{O}_{2}$ in Pa

### 7.2 Activity coefficient of water and $\mathrm{H}_{2} \mathrm{O}_{2}$

Hydrogen peroxide and water interact with each other in a vapor mixture; therefore the mixture will not comply with an ideal solution model. To account for the deviation from ideal behavior, we use activity coefficients. The activity coefficients $Y_{w}\left(\right.$ for $\left.\mathrm{H}_{2} \mathrm{O}\right)$ and $Y_{h}\left(\right.$ for $\left.\mathrm{H}_{2} \mathrm{O}_{2}\right)$ can be calculated with the following formulas by Scatchard et. al. [2]:

$$
\begin{align*}
& \gamma_{w}=\exp \left\{\frac{\left(1-x_{w}\right)^{2}}{R T} \cdot\left[B_{0}+B_{1}\left(1-4 x_{w}\right)+B_{2}\left(1-2 x_{w}\right) \cdot\left(1-6 x_{w}\right)\right]\right\} \text { and }  \tag{Equation10}\\
& \gamma_{h}=\exp \left\{\frac{x_{w}^{2}}{R T} \cdot\left[B_{0}+B_{1}\left(3-4 x_{w}\right)+B_{2}\left(1-2 x_{w}\right) \cdot\left(5-6 x_{w}\right)\right]\right\}, \text { where } \tag{Equation11}
\end{align*}
$$

$R=$ Universal gas constant $1.986 \mathrm{cal} \cdot \mathrm{K}^{-1} \cdot \mathrm{~mol}^{-1}$
Table 3: Numerical values for coefficients $B_{0} \ldots B_{2}$

| Coefficients $\mathrm{B}_{\mathrm{n}}$ | For water $+\mathrm{H}_{2} \mathrm{O}_{2}$ solution |
| :---: | :---: |
| $\mathrm{B}_{0}$ | $-752+0.97 \cdot T\left[\mathrm{cal} \cdot \mathrm{mol}^{-1}\right]$ |
| $\mathrm{B}_{1}$ | $85\left[\mathrm{cal} \cdot \mathrm{mol}^{-1}\right]$ |
| $\mathrm{B}_{2}$ | $13\left[\mathrm{cal} \cdot \mathrm{mol}^{-1}\right]$ |

### 7.3 Mole fraction of water and $\mathrm{H}_{2} \mathrm{O}_{2}$

Raoult's law states that in a chemical mixture, the sum of mole fractions of all mixture components must be equal to one. Therefore, in the case of a mixture containing both water and $\mathrm{H}_{2} \mathrm{O}_{2}$ :
$x_{h}+x_{w}=1$
(Equation 12)

In liquid solutions, the mole fraction of $\mathrm{H}_{2} \mathrm{O}_{2}\left(X_{h}\right)$ can be calculated as a fraction amount of a substance:
$x_{h}=\frac{n_{h}}{n_{h}+n_{w}} \quad$, where
(Equation 13)
$n_{h}=$ Amount of substance for $\mathrm{H}_{2} \mathrm{O}_{2}$ in mol
$n_{w}=$ Amount of substance for water in mol

The amount of $\mathrm{H}_{2} \mathrm{O}_{2}$ can be calculated using the equation below. A similar equation can also be used for calculating the amount of $\mathrm{H}_{2} \mathrm{O}$.
$n_{h}=\frac{w-\%_{\mathrm{H} 2 \mathrm{O} 2}}{M_{\mathrm{H} 2 \mathrm{O} 2}}$, where
(Equation 14)
$w-\%_{\mathrm{H}_{2} \mathrm{O} 2}=\mathrm{H}_{2} \mathrm{O}_{2}$ liquid concentration in mass percent
$M_{\mathrm{H}_{2} \mathrm{O} 2}=$ Molecular weight of chemical $\mathrm{H}_{2} \mathrm{O}_{2}$ in $\mathrm{g} \cdot \mathrm{mol}^{-1}$
In vapor mixtures of $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{O}_{2}$, mole fractions behave differently compared to liquids. In the case of vaporized mixtures, mole fraction cannot be calculated using equations 13 and 14 , which apply to liquids. At condensation, when the vapor starts to saturate i.e.: form droplets, the mole fraction can be different depending on the temperature, water, and $\mathrm{H}_{2} \mathrm{O}_{2}$ concentrations. Therefore, the mole fraction in the vapor phase must be determined using an iterative procedure.

### 7.4 Iterative calculation for $\mathrm{P}_{\mathrm{ws}}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$

In order to calculate water vapor saturation pressure $P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ in an $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor environment, we need to find mole fractions from equations 8 and 9:
$x_{w}=\frac{P_{w}}{\gamma_{w} P_{w s}}$ and $x_{h}=\frac{P_{h}}{\gamma_{h} P_{h s}}$
(Equations 15, 16)

We then combine equations 15 and 16 with equation 12 to find water vapor pressure $\left(P_{w}\right)$ :
$P_{w}=\gamma_{w} P_{w s}\left(1-\frac{P_{h}}{\gamma_{h} P_{h s}}\right) \stackrel{\text { rename }}{\Longrightarrow} P_{m s}$
(Equation 17)

To be unambiguous, let us rename this water vapor pressure as "mixture water vapor pressure" ( $P_{m s}$ ).

There are now two equations presented for water vapor pressure (equations 8,17 ) and one unknown variable (mole fraction of water $x_{w}$ ). Both equations 8 and 17 should produce the same value for water vapor pressure. The Mole fraction of water can be solved by using an iterative procedure shown in the flow diagram below. By using iterated mole fraction $x_{h}$, water vapor can be calculated using equation 17 or 8 . The calculated water vapor pressure indicates the water vapor saturation pressure in a vaporized $\mathrm{H}_{2} \mathrm{O}_{2}$ environment, $\mathrm{P}_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$. A similar calculation is presented by Parks et al [3].


| Iteration |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Step | $\mathrm{X}_{\mathrm{h}} \mathbf{\operatorname { m i n }}{ }^{\circ} \mathrm{C}$ | $\mathrm{X}_{\mathrm{h}} \max { }^{\circ} \mathrm{C}$ | $\mathrm{X}_{\mathrm{h}}$ average ${ }^{\circ} \mathrm{C}$ | $\boldsymbol{P}_{w} \mathbf{P}_{\text {a }}$ | $\boldsymbol{P}_{\boldsymbol{m s}} \mathbf{P}_{\mathrm{a}}$ |
| 1 | O [initial] | 1 [initial] | 0.50 | 1038.89 | 823.27 |
| 2 | 0 | 0.5 | 0.25 | 917.34 | 1596.25 |
| 3 | 0.25 | 0.5 | 0.375 | 1056.50 | 1190.28 |
| 4 | 0.375 | 0.5 | 0.438 | 1062.04 | 999.89 |
| 5 | 0.375 | 0.438 | 0.406 | 1063.45 | 1093.57 |
| 6 | 0.406 | 0.438 | 0.422 | 1063.71 | 1046.32 |
| 7 | 0.406 | 0.422 | 0.414 | 1063.83 | 1069.85 |
| 8 | 0.414 | 0.422 | 0.418 | 1063.83 | 1058.06 |
| .. | .. | .. | . | .. | . |
| 19 | 0.416 | 0.416 | 0.416 | 1063.85 | 1063.85 |
| 20 | 0.416 | 0.416 | 0.416 | 1063.85 | 1063.85 |

Answer: $P_{m s}=P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)=1068.85 \mathrm{~Pa}$

## 8. Dew point in an $\mathrm{H}_{2} \mathrm{O}_{2}$ environment - $\mathrm{T}_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$

The dew point temperature ( $T_{d}$ ) is the temperature to which air must be cooled to become saturated with water vapor. The term $T_{d}$ is valid when dew point temperature is equal to or above $0^{\circ} \mathrm{C}$. When $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor is present in the air mixture, deriving the dew point from only the water vapor is insufficient because the $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor will change the dew point. This is because $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor effects the water vapor saturation pressure, $P_{w s}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$; with an increase in $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor, the water vapor saturation pressure will decrease. In other words, when the $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor concentration is increased, the maximum amount of water vapor that the air can hold decreases. In order to distinguish dew point derived from only water ( $T_{d}$ ), let's abbreviate this mixture dew point $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ which indicates the dew point temperature in an $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor environment.

### 8.1 Dew point to vapor pressure - $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ to $P_{w}$ and $P_{h}$

Calculating the vapor pressure from $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ is a straightforward operation. For water vapor pressure, use equation 8 to calculate the water vapor saturation pressure, mole fraction and activity coefficient in $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ condition:
$P_{w}\left(T_{K}\right)=\gamma_{w}\left(T_{d}+273.15\right) \cdot x_{w}\left(T_{d}+273.15\right) \cdot P_{w s}\left(T_{d}+273.15\right)$
(Equation 18)
For $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor pressure, use equation 9 to calculate the $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor saturation pressure, mole fraction and activity coefficient in $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ condition:
$P_{h}\left(T_{K}\right)=\gamma_{h}\left(T_{d}+273.15\right) \cdot x_{h}\left(T_{d}+273.15\right) \cdot P_{h s}\left(T_{d}+273.15\right)$ (Equation 19)

When $\operatorname{ppm}_{\mathrm{H} 2 \mathrm{O} 2}=0 \mathrm{ppm}_{v}$, then $Y_{w}=1, X_{w}=1$ and $x_{h}=0$ and both equation above simplify. Therefore, at that point $T_{d}=T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$.

### 8.2 Vapor pressure to dew point - $P_{w}$ and $P_{h}$ to $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$

Calculating dew point from vapor pressure, temperature, and pressure involves complex equations, because the mole fraction, activity coefficient, and vapor pressure are dependent on the dew point result. Dew point can be solved by using an iterative procedure.

Initial values for a trial-and-error process should be wide enough to accommodate the result within its boundaries. Proper values for the majority of applications are between $0^{\circ} \mathrm{C} \ldots 100^{\circ} \mathrm{C}$. The vapor pressure to dew point iterative process is shown in the flow diagram below:


## Example:

To calculate $T_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)$ in following condition:

```
ppm
T = 20 }\mp@subsup{}{}{\circ}\textrm{C}=> \mp@subsup{T}{\textrm{k}}{}=293.15\textrm{K
RH = 42.0 %rh
p = 101325 P
P
```

Answer: $\mathrm{T}_{d}\left(\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O}_{2}\right)=19.35^{\circ} \mathrm{C}$

## 9. Absolute concentration of water and $\mathrm{H}_{2} \mathrm{O}_{2}-a_{w}$ and $a_{h}$

Absolute concentration of water - also called absolute humidity - is defined as the mass of water vapor in a certain volume. In the case of $\mathrm{H}_{2} \mathrm{O}_{2}$, absolute hydrogen peroxide is defined as the mass of $\mathrm{H}_{2} \mathrm{O}_{2}$ vapor in a certain volume. If ideal gas behavior is assumed, the absolute concentration can be calculated using:

$$
\begin{equation*}
a_{x}=\frac{M_{x} \cdot P_{x}}{R \cdot T_{K}}, \text { where } \tag{Equation20}
\end{equation*}
$$

$a_{x}=$ Absolute concentration of chemical $X$ in $g \cdot \mathrm{~m}^{-3}$
$M_{x}=$ Molecular mass of chemical $X$ in $g \cdot \mathrm{~mol}^{-1}$
$R=$ Universal gas constant $8.3145 \mathrm{~J} \cdot \mathrm{~K}-1 \cdot \mathrm{~mol}^{-1}$
$P_{x}=$ Vapor pressure of chemical $X$ in Pa
$T_{K}=$ Temperature in K

## Example:

To calculate absolute humidity in following condition:

$$
\begin{aligned}
R H & =42.0 \% \mathrm{rh} \\
T & =20^{\circ} \mathrm{C}=>\mathrm{T}_{\mathrm{K}}=293.15 \mathrm{~K} \\
p & =101325 \mathrm{~Pa} \\
M_{\text {H2O }} & =18.0146 \mathrm{~g} \cdot \mathrm{~mol}^{-11} \\
P_{w S}(5) & =2339.25 \mathrm{~Pa} \\
P_{w}(1) & =982.26 \mathrm{~Pa}
\end{aligned}
$$

$$
a_{w}=\frac{M_{\mathrm{H} 2 O} \cdot P_{w}}{R \cdot T_{K}}=\frac{18.0146 \mathrm{~g} \cdot \mathrm{~mol}^{-1} \cdot 982.26 \mathrm{~Pa}}{8.3145 \mathrm{~J} \cdot \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \cdot 293.15 \mathrm{~K}}=7.3 \mathrm{~g} \cdot \mathrm{~m}^{-3}
$$

To calculate absolute $\mathrm{H}_{2} \mathrm{O}_{2}$ in following condition:

$$
\begin{aligned}
p p m_{V ~ H 2 O 2} & =500 \mathrm{ppm} \\
T & =20^{\circ} \mathrm{C}=>\mathrm{T}_{\mathrm{K}}=293.15 \mathrm{~K} \\
T & =101325 \mathrm{~Pa} \\
p & =34.0136 \mathrm{~g} \cdot \mathrm{~mol}^{-11} \\
M_{H 2 O 2} & \\
P_{h}(1) \quad & 50.66 \mathrm{~Pa} \\
a_{h} & =\frac{M_{H 2 O 2} \cdot P_{h}}{R \cdot T_{K}}=\frac{34.0136 \mathrm{~g} \cdot \mathrm{~mol}^{-1} \cdot 50.66 \mathrm{~Pa}}{8.3145 \mathrm{~J} \cdot \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \cdot 293.15 \mathrm{~K}}=0.70699 \mathrm{~g} \cdot \mathrm{~m}^{3}=707.0 \mathrm{mg} \cdot \mathrm{~m}^{-3}
\end{aligned}
$$

## 10. Molecular weight

The molecular weight (molar mass $M$ ) of a substance is needed in mass-based calculations, such as absolute concentrations and ppm concentration in mass fraction. Molecular mass of a substance is the sum of the mole fractions of its gas components multiplied by their molar mass. See "Atomic weights of the elements 2013" by J. Meija et al. [4]. Let us take dry air as an example. There are seasonal variations in the composition of the air as well as a continuous change, especially in the $\mathrm{CO}_{2}$ content. Here is a 4-component simplification of dry air:

| Component | Molar ratio <br> $\left(\mathrm{mol}^{\prime} \mathrm{mol}_{\text {eir }}{ }^{-1}\right)$ | Molar mass <br> $\left(\mathrm{g} \cdot \mathrm{mol}^{-1}\right)$ | Molar mass in air <br> $\left(\mathrm{g} \cdot \mathrm{mol}_{\text {air }}{ }^{-1}\right)$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{N}_{2}$ | 0.7808 | 28.013 | 21.872 |
| $\mathrm{O}_{2}$ | 0.2095 | 31.999 | 6.7037 |
| Ar | 0.0093 | 39.948 | 0.3715 |
| $\mathrm{CO}_{2}$ | 0.0004 | 44.01 | 0.0176 |
| Total | 1 |  | 28.965 |

The molar mass of air is $28.965 \mathrm{~g} \cdot \mathrm{~mol}^{-1}$.

Other gas mixtures can be calculated by using a similar method.

The chemical formula of water is $\mathrm{H}_{2} \mathrm{O}$, which means that each molecule contains one oxygen and two hydrogen atoms. Similarly, the chemical formula of hydrogen peroxide is $\mathrm{H}_{2} \mathrm{O}_{2}$, which means that each molecule contains two oxygen and two hydrogen atoms.

| Component | Molar mass <br> $\left(\mathrm{g} / \mathrm{mol}^{-1}\right)$ |
| :---: | :---: |
| $H$ | 1.0078 |
| O | 15.999 |
| $\mathrm{M}_{\mathrm{H} 2 \mathrm{O}}$ | 18.0146 |
| $M_{\mathrm{H} 2 \mathrm{O} 2}$ | 34.0136 |

The molar mass of water is $18.0146 \mathrm{~g} \cdot \mathrm{~mol}^{-1}$ and molar mass of hydrogen peroxide is $34.0136 \mathrm{~g} \cdot \mathrm{~mol}^{-1}$.

## 11. Conversions to Imperial units and non-SI units

- Fahrenheit temperature: $T_{{ }^{\circ} F}=T_{{ }^{\circ} C} \cdot \frac{9}{5}+32$
- psi (pounds per square inch): $p_{p s i}=6894.76 \cdot p_{P a}$
- Absolute concentration in grains per cubic feet: $A_{g r / f t 3}=2.2883 \cdot A_{g / \mathrm{kg}}$
- Conversion from $\mathrm{ppm}_{\mathrm{v}}$ to milliliters per cubic meter: $1 \mathrm{ppm}_{v}=1 \frac{\mathrm{~mL}}{\mathrm{~m}^{3}}$


## 12. References

[1] D. Sonntag, "The history of formulations and measurements of saturation water vapour pressure," in Papers and abstracts from the Third International Symposium on Humidity and Moisture, vol. 1, Teddington, 1998.
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[3] D. W. M. Parks, "The Relationship between Saturated Hydrogen Peroxide, Water Vapour and Temperature," Pharmaceutical Technology Europe, 2004.
[4] J. Meija, T. B. Coplen, M. Berglund, W. A. Brand, P. De Bièvre, M. Gröning, N. E. Holden, J. Irrgeher, R. D. Loss, T. Walczyk and T. Prohanska, "Atomic weights of the elements 2013," IUPAC, 2015.

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[^0]:    'See chapter 10 Molecular weight

